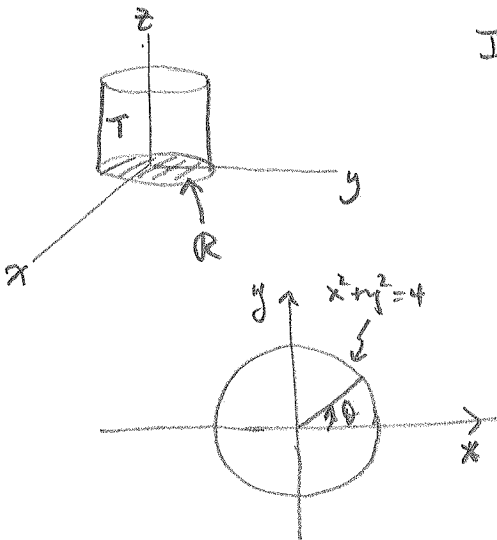


$$2 \quad b). \quad J = \int_0^1 \int_0^z y^2 z \, dy \, dz = \int_0^1 \frac{1}{3} z^4 \, dz = \frac{1}{15}$$

7. [5 marks] Evaluate the iterated integral  $\iiint_T e^{x^2+y^2} \, dV$  where  $T$  is the solid bounded by the cylinder  $x^2 + y^2 = 4$  and the planes  $z = 0$  and  $z = 4$ .

Use cylindrical coordinates. ← ①



$$\begin{aligned} I &= \iiint_T e^{x^2+y^2} \, dV \\ &= \iint_R \int_{z=0}^{z=4} e^{x^2+y^2} \, dV \\ &= \int_0^{2\pi} \int_0^2 \int_0^4 r e^{r^2} \, dz \, dr \, d\theta \end{aligned}$$

$$R = \{(r, \theta) : 0 \leq r \leq 2, 0 \leq \theta \leq 2\pi\}$$

$$\begin{aligned} &= \dots \\ &= 4\pi(e^4 - 1) \end{aligned}$$

↑  
①