

Part B: [15 marks] Two moles of an ideal gas with molar heat capacity $C_{v,m} = 3R/2$, initially confined to a container of volume 6 L and at a temperature 298.15 K, irreversibly expand (or are compressed) against a constant external pressure of 7.10 atm until the final pressure of the gas is equal to the external pressure and the final temperature of the gas is equal to the temperature of the surroundings. During this process the system does 4000 J of work on the surroundings. (**Note:** 1 L = 1.0×10^{-3} m³)

(a) [5 marks] Evaluate the volume and temperature of the final state of the system.

$$(a) \left\{ \begin{array}{l} w = -p_{ex} \cdot \Delta V = -p_f \cdot \Delta V \Rightarrow \Delta V = -\frac{w}{p_f} = -\frac{-4000 \times 10^3}{7.10 \times 101325} = 5.56 \text{ L} \\ \Delta V = V_f - V_i \Rightarrow V_f = \Delta V + V_i = 5.56 + 6 = 11.56 \text{ L} \quad (1.156 \times 10^{-2} \text{ m}^3) \\ p_f V_f = nRT_f \Rightarrow T_f = \frac{p_f V_f}{nR} = \frac{7.10 \times 11.56}{2 \times 0.08206} = 500.1 \text{ K} \quad (227^\circ\text{C}) \\ \text{or: } T_f = \frac{p_f V_f}{nR} = \frac{7.10 \times 101325 \times 11.56 \times 10^{-3}}{2 \times 8.314} = 500.1 \text{ K} \quad (227^\circ\text{C}) \end{array} \right.$$

(b) [10 marks] Calculate ΔU , ΔH , ΔS , and q for this process.

$$(b) \left\{ \begin{array}{l} \Delta T = T_f - T_i = 500.1 - 298.15 = 202 \text{ K} \\ \Delta U = nC_{v,m} \Delta T = 2 \frac{3R}{2} \Delta T = 2 \times \frac{3 \times 8.314}{2} \times 202 \text{ J} = 5.04 \text{ kJ} \quad (5038 \text{ J}) \\ q = \Delta U - w = 5.04 - (-4) = 9.04 \text{ kJ} \quad (9038 \text{ J}) \\ \Delta H = nC_{p,m} \Delta T = 2 \frac{5R}{2} \Delta T = 2 \times \frac{5 \times 8.314}{2} \times 202 \text{ J} = 8.40 \text{ kJ} \quad (8397 \text{ J}) \end{array} \right.$$

$$\left\{ \begin{array}{l} \Delta S = nC_{v,m} \ln \frac{T_f}{T_i} + nR \ln \frac{V_f}{V_i} \\ = 2 \times \frac{3 \times 8.314}{2} \times \ln \frac{500.1}{298.15} + 2 \times 8.314 \times \ln \frac{11.56}{6} = 23.8 \text{ J/K} \end{array} \right.$$

$$\text{or: } \left\{ \begin{array}{l} p_i V_i = nRT_i \Rightarrow p_i = \frac{nRT_i}{V_i} = \frac{2 \times 0.08206 \times 298.15}{6} = 8.16 \text{ atm} \\ \Delta S = nC_{p,m} \ln \frac{T_f}{T_i} + nR \ln \frac{p_i}{p_f} = 5R \ln \frac{500.1}{298.15} + 2R \ln \frac{8.16}{7.10} = 23.8 \text{ J/K} \end{array} \right.$$

Part C: [12 marks] Consider the following reaction (**Note:** $0\text{ }^{\circ}\text{C} = 273.15\text{ K}$):



(a) [6 marks] Use the following table to calculate ΔH^0 , ΔS^0 , and ΔG^0 of the above reaction at $25\text{ }^{\circ}\text{C}$:

| | $\Delta H_{\text{f,m}}^0$ [kJ mol ⁻¹] | $S_{\text{f,m}}^0$ [J K ⁻¹ mol ⁻¹] |
|---------------------|---|---|
| C (s, diamond) | 1.895 | 2.377 |
| CH ₄ (g) | -74.810 | 186.260 |
| H ₂ (g) | | 130.700 |

$$(a) \left\{ \begin{array}{l} \Delta H^0 = 1.895 - (-74.810) = 76.705 \text{ kJ (76705 J)} \\ \Delta S^0 = 2.377 + 2 \times 130.700 - 186.260 = 77.517 \text{ J/K} \\ \Delta G^0 = \Delta H^0 - T \cdot \Delta S^0 = 76705 - 298.15 \times 77.517 \text{ J} = 53.60 \text{ kJ (53593 J)} \end{array} \right.$$

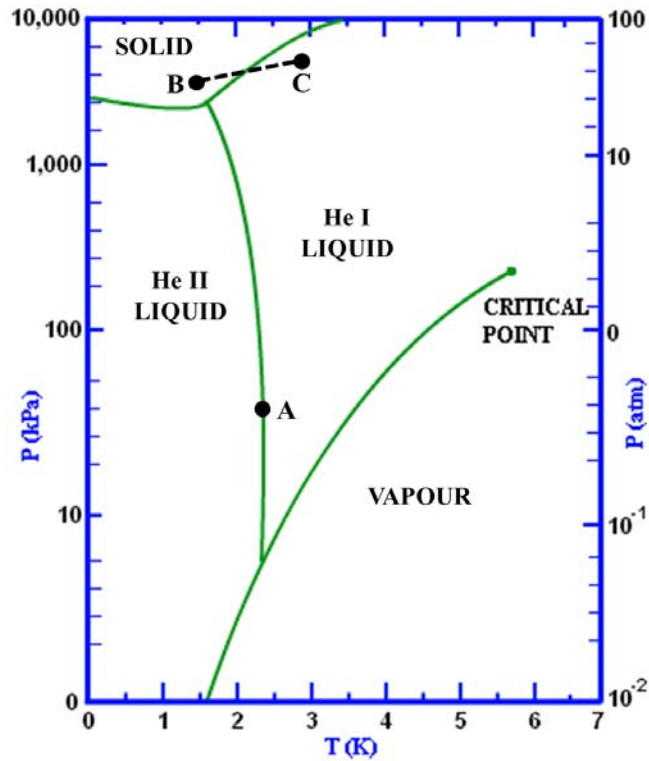
(b) [3 marks] Calculate the equilibrium constant, K , of the above reaction at $25\text{ }^{\circ}\text{C}$. Is this reaction spontaneous at $25\text{ }^{\circ}\text{C}$ and under 1 atm partial pressure for all gases? Justify your answer.

$$(b) \left\{ \begin{array}{l} \Delta G^0 = -RT \ln K \Rightarrow \ln K = \frac{-\Delta G^0}{RT} = \frac{-53.60 \times 10^3}{8.314 \times 298.15} = -21.6 \\ K = e^{-21.6} = 4 \times 10^{-10} \\ \text{Everything is in standard state} \Rightarrow Q = 1 \Rightarrow \Delta G = \Delta G^0 > 0 \\ \text{Forward reaction is not spontaneous, because } \Delta G^0 > 0 \text{ or } K < 1. \end{array} \right.$$

(c) [3 marks] In a galaxy far, far away, scientists recently discovered an alien planet. It has been observed that its atmosphere contains $\text{CH}_4(\text{g})$ and $\text{H}_2(\text{g})$ and its surface temperature can reach $900\text{ }^{\circ}\text{C}$ during some period of the day. Can it rain diamonds on that planet at $900\text{ }^{\circ}\text{C}$ and under 1 atm partial pressure for all gases? Assume ΔH^0 and ΔS^0 are both independent of the temperature. Justify your answer.

$$(c) \left\{ \begin{array}{l} \text{Assume } \Delta H^0 \text{ and } \Delta S^0 \text{ are both independent of } T: \\ \Delta G_{900^{\circ}\text{C}}^0 = \Delta H^0 - T \cdot \Delta S^0 = 76705 - 1173.15 \times 77.517 \text{ J} = -14.2 \text{ kJ (-14234 J)} \\ \text{Everything is in standard state (} Q = 1 \text{)} \Rightarrow \Delta G_{900^{\circ}\text{C}} = \Delta G_{900^{\circ}\text{C}}^0 < 0 \\ \text{Thus, forward reaction becomes spontaneous.} \\ \text{Therefore, it can rain diamonds at } 900^{\circ}\text{C} \text{ \& standard states.} \end{array} \right.$$

Part D: [3 marks] In the phase diagram for helium (He) below, there are two distinct liquid phases, “He I” and “He II”, in addition to the solid phase and vapour phase.



(a) [1 mark] The broken line connecting points **B** and **C** signifies a constant-volume process between the solid (**B**) and the liquid He I (**C**) phases, **B** → **C**. Should the change in internal energy (ΔU) for **B** → **C** be positive, negative, or zero? (circle one below)

1) positive 2) negative 3) zero

$$(a) \Delta T_{B \rightarrow C} > 0 \Rightarrow q_V = C_V \cdot \Delta T_{B \rightarrow C} > 0 \Rightarrow \Delta U = q_V > 0$$

(b) [1 mark] At point **A** on the boundary curve separating the two liquid phases, is $\Delta S_{\text{universe}}$ positive, negative, or zero for the phase transition: He I (*l*) → He II (*l*) at constant pressure? (circle one below)

1) positive 2) negative 3) zero

$$(b) \Delta G_A = 0 \Rightarrow \Delta S_{\text{universe}} = 0$$

(c) [1 mark] At point **A** on the boundary curve separating the two liquid phases, is ΔS_{system} positive, negative, or zero for the phase transition: He I (*l*) → He II (*l*) at constant pressure? (circle one below)

1) positive 2) negative 3) zero

$$(c) \Delta H_{I \rightarrow II} < 0 \Rightarrow \Delta S_A = \frac{\Delta H_{I \rightarrow II}}{T_A} < 0$$