

## MECH 331 Fluids I

Fall 2013

Instructor: Prof. Tim Lee, MC 211, [tim.lee@mcgill.ca](mailto:tim.lee@mcgill.ca)  
 Lecture: M W F 9:30 - 10:30, ENGMD280  
 Tutorial:  
**Office hours:** M W F 10:35 - 11:35, MC211  
 Textbook: *Introduction to Fluid Mechanics*, Fox, Pritchard and McDonald, 7<sup>th</sup> Ed.  
 T.A.: Ying Y. Su ([ying.su@mail.mcgill.ca](mailto:ying.su@mail.mcgill.ca)); MD162

## COURSE CONTENTS

Introduction and fundamental concepts	(Chapters 1 & 2)
Basic equations in integral form for a control volume	(Chapter 4)
Fluid statics	(Chapter 3)
Introduction to differential analysis of fluid motion	(Chapter 5)
Incompressible inviscid flow	(Chapter 6)
Dimensional analysis and similitude	(Chapter 7)
Internal incompressible viscous flow	(Chapter 8)
External incompressible viscous flow	(Chapter 9)
Fluid machinery	(Chapter 10; tentative)

## Q/A EXERCISE

A part of class time will be used to practice problem solving skills with peer and instructor interaction. During these sessions a problem will be assigned to the entire class. You will be asked for inputs for the solution.

## GRADING POLICY

Homework assignments (not collected)  
**Midterm 1** (9:30-10:30, Monday, **Oct. 7**, closed books/note)  
**Midterm 2** (9:30-10:30, Monday, **Nov. 11**, closed books/note)  
**Final exam**\* (3-hour exam)

Handouts A1 + A2  
 25%  
 25%  
 50% of 75%

\*Students are allowed to drop one midterm and make final 75% (a maximum).

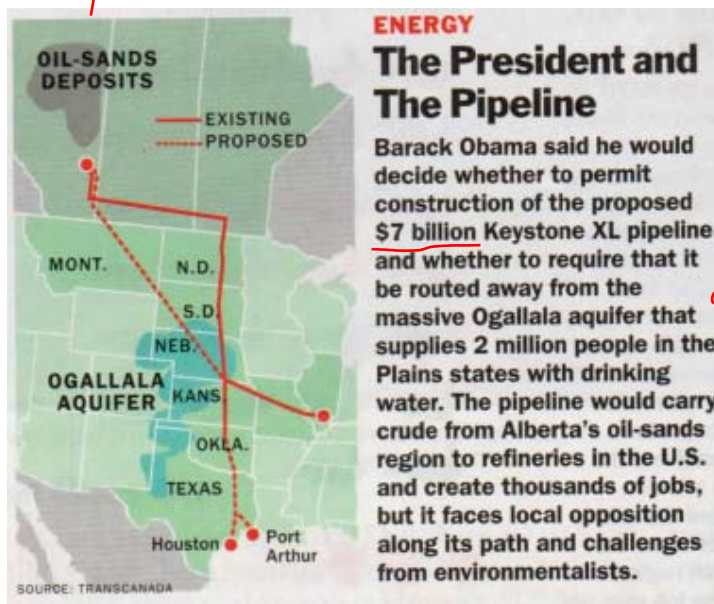
## Scope and application of fluid mechanics

- Aerodynamics of airplanes and road vehicles
- Design of fluid systems and devices
- Aerodynamics of sports
- Bioengineering
- Others

SUBSONIC  
|  
SUPERSONIC

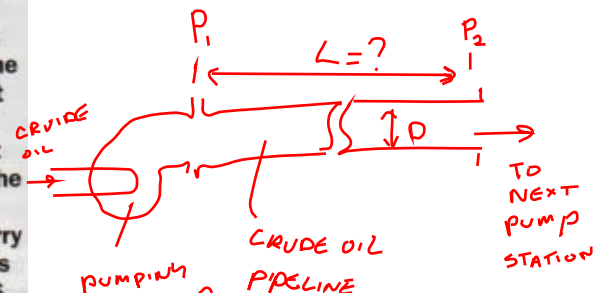
GOLF BALL  
BASEBALL

E.G.,



TIME November 14, 2011

2,148 mi LONG,  $D = 36''$  DIA,  
590,000 BPD



pumping power = ?

FROM CHAP. 8 INT, INCOMP. VISCIOUS FLOW

1 BARREL = 42 GALLONS

1 GALLON = 3.78 LITERS

The most significant basic equations in MECH 331 ( $\rho = \text{CONST.}$   $T = \text{CONST.}$  incompressible and isothermal flow)

1. Reynolds Transport Theorem (integral form of  $\sum \bar{F} = m \frac{d\bar{V}}{dt}$ )

$$\left( \begin{array}{l} \text{The sum of all} \\ \text{forces acting} \\ \text{on a system} \end{array} \right) = \left( \begin{array}{l} \text{The rate of change} \\ \text{of momentum inside} \\ \text{a control volume} \end{array} \right) + \left( \begin{array}{l} \text{The net rate of flux} \\ \text{of momentum out through} \\ \text{the control surface} \end{array} \right)$$

$$\sum \bar{F} = \sum \bar{F}_{\text{surface}} + \sum \bar{F}_{\text{body}} \quad \frac{\partial}{\partial t} \int_{CV} \bar{V} \rho dV \quad \int_{CS} \bar{V} \rho \bar{V} \cdot d\bar{A}$$

$\bar{V} = u\hat{i} + v\hat{j} + w\hat{k} = \vec{V}(x, y, z, t)$   
 PRESSURE FORCE + VISCIOUS FORCE

2. Navier-Stokes equations (differential form of  $\sum \bar{F} = m \frac{d\bar{V}}{dt}$ )

The sum of all forces acting on a fluid particle	=	Pressure force acts on a fluid particle per unit volume	+	Body force acts on a fluid particle per $dV$	+	Viscous force acts on a fluid particle per unit volume
$\rho \frac{D\bar{V}}{Dt} dV$		$-\nabla P dV$		$\rho \bar{g} dV$		$\mu \nabla^2 \bar{V} dV$

$dV = dx dy dz$

$\nabla = \frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial z}$

$\mu = \text{FLUID VISCOSITY}$   
 $\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}$

= DEL OPERATOR

3. Bernoulli equation (for non-viscous flow)

$$\frac{P}{\rho} + \frac{V^2}{2} + gz = \text{Constant}$$

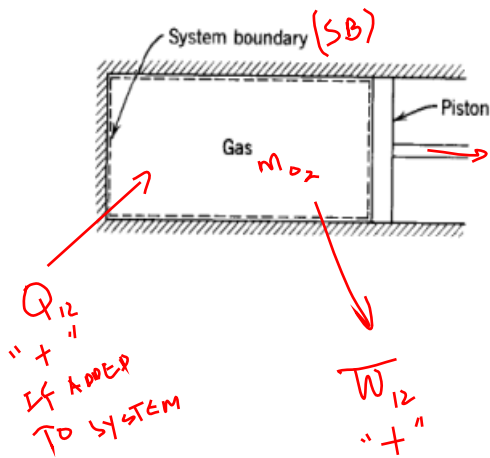
∴ IF  $\Delta z \approx 0$

THEN  $\uparrow$  IN P IS ACCOMPANIED BY  $\downarrow$  IN V  
 VICE VERSA

## Method of motion analysis

### System approach

- A system is defined as a fixed, identifiable quantity of mass.
- System boundary separates the system from the surrounding (SB)
- No  $\dot{m}$  crosses the system boundary



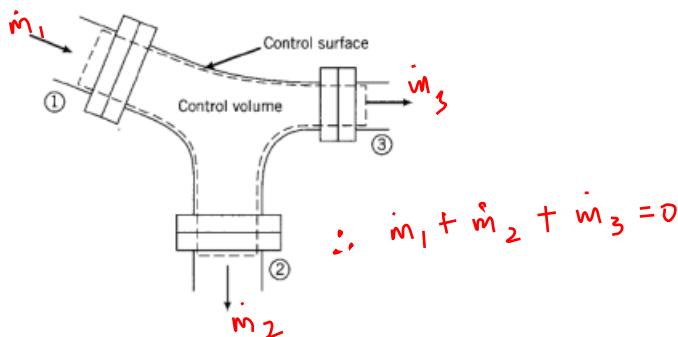
GIVEN:  $P_1 = P_2$ ,  $T_1 \neq T_2$ ,  $m_{O_2}$ ,  $P = \rho R T$   
 FIND:  $Q_{12}$

SOLN:  $Q_{12} - \overline{W}_{12} = m c_v (T_2 - T_1)$

$\therefore Q_{12} = m c_p (T_2 - T_1)$   $\int_{T_1}^{T_2} P dV = P \Delta V = m R \Delta T$   
 $c_p - c_v$

### Control volume approach

- A control volume is defined as an arbitrary volume in space through which the fluid flows.
- Control surfaces are the geometric boundary of the control volume. (CS)  
 Control surface can be at rest or in motion.  
 Control surface can be real or imaginary
- Advantages and drawbacks over the system approach

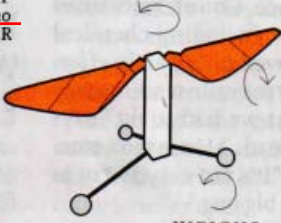


## Some icebreaking Q/As and fundamental concepts

**THE FUTURE**

**THE ROBOBEE**  
Harvard's School of Engineering and Applied Sciences conducted the first successful flight of a life-size robotic fly in 2007. The lab has received **\$10 million** in grant money from the National Science Foundation to build a network of autonomous artificial bees.

ARTIFICIAL MUSCLES CAN BEAT WINGS 120 TIMES PER SECOND



AIRFOILS ROTATE INDEPENDENTLY

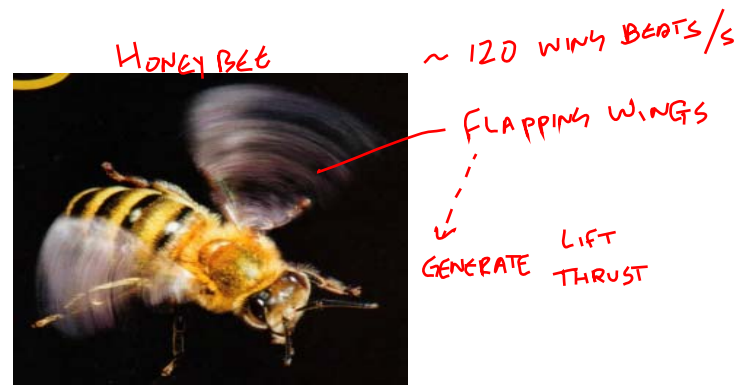
WEIGHS 80 MC

**APPLICATIONS**

- SEARCH AND RESCUE
- ARTIFICIAL POLLINATION
- COVERT SURVEILLANCE
- HIGH-RESOLUTION WEATHER AND CLIMATE MAPPING
- TRAFFIC MONITORING

Time (Aug 19, 2013)

∴ MASS BEE DEATH



## Hummingbird NAV

↳ DARPA \$4M PROGRAM



AeroVironment Hummingbird (2011) with landing gear



AeroVironment Hummingbird displaying its maneuverability:  $b = 19 \text{ cm}$ ,  $W_{\text{total}} = 19 \text{ g}$ ,  $V = 11 \text{ mph}$ , Duration  $\sim 11$  minutes.

\$15,000 EACH  
\$300,000 UAS

H-P FLAPPING-WING AIRCRAFT

"Snowbird" Human-Powered Ornithopter (HPO)



Aug. 2, 2010

19.3 sec  
25.6 km/h

$$D_{TOTAL} = D_i + D_p + D_{PARASITE}$$



$$W_{TO} = 43.5 + 70.8 \text{ kg}$$

$$\begin{matrix} W_e \\ W_{PILOT} \end{matrix}$$

$$\begin{aligned} b &= 32 \text{ m} \\ f &= 0.65 \text{ Hz} \\ P_{FLIGHT} &= 600 \text{ W} \\ AR &= \frac{b^2}{S} = 35 \\ \frac{L}{D} &= 20.7 \end{aligned}$$

"Atlas" Human-Powered Helicopter (HPH)

\$250,000  
SIKORSKI  
PRIZE



φ 66.2'



July, 2013

$W_e = 122 \text{ lb}$   
ALOFT 65 sec  
ALTITUDE 3.3 m  
WITHIN 10-m BOX

$P = 1.1 \text{ kW} \rightarrow 600 \text{ W}$

Q/A: WHAT IS FLAPPING WING ?

Q/A: HOW FLAPPING WINGS GENERATE LIFT & THRUST ?

Q/A: ADVANTAGES/SHORTCOMINGS OVER FIXED-WING FLIGHT ?

HOW TO ESTIMATE THE POWER ADD ? ?

FROM CHAPT. 4

CONTROL-VOLUME METHOD ANALYSIS.

**TF-X: Terrafugia's four-passenger, hybrid-electric roadable aircraft**



Terrafugia's four-passenger, hybrid-electric automobile



In takeoff or landing mode, the TF-X is a stop/fold tiltrotor with two 600-hp electric motors in nacelles at the tips of the wings.



In flight mode, the TF-X uses a 300-hp ducted fan for thrust, giving a non-stop range of 500 mi.

$U_c = 200 \text{ pmh}$   
 RANGE 500 mi  
 $< 19,000 \text{ lb}_f$

**Terrafugia Transition: A light sport roadable aircraft**



Automobile configuration



Airplane configuration  
 APRIL, 2012 (8 min @ 1,400')  
 \$ 279,000 EACH

$b = 26'6''$   
 $U_c = 105 \text{ mph}$   
 RANGE = 490 mi  
 TO LENGTH = 1,700'  
 $\bar{W}_{TO} = 1,430 \text{ kg}$

Bell-Boeing V-22 Osprey "FLY LIKE A BIRD, HOVER LIKE A BEE."



ROTOR DIA.  $\phi 38'$   
 TILTS  $97^\circ$  IN 30 SEC  
 $W_{TO} = 60,500 \text{ lb}_f$   
 $U_c \sim 300 \text{ mph}$   
 24 - 30 TROOPS  
 RANGE 1,100 mi  
 $\sim \$40B$  R&D COSTS

Q/A: Advantages and drawbacks of V-22 aircraft?

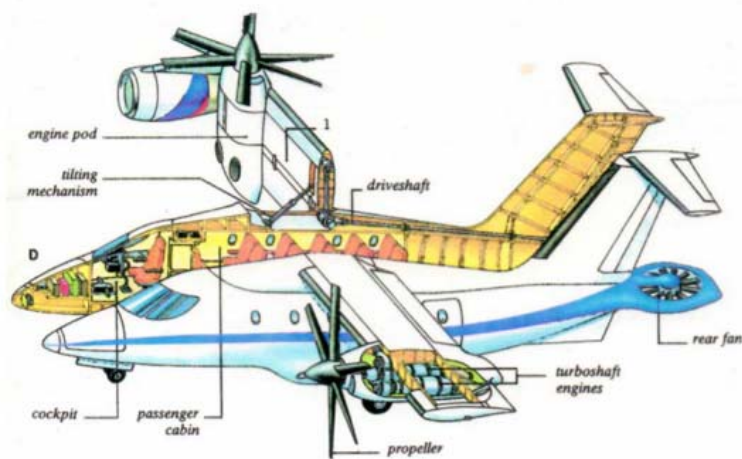
Q/A: Advantages and disadvantages over tiltwing aircraft?

Q/A: V-22 compared to Bell V-280 Valor tiltrotor concept

## Tiltwing aircraft

ADVANTAGES ?

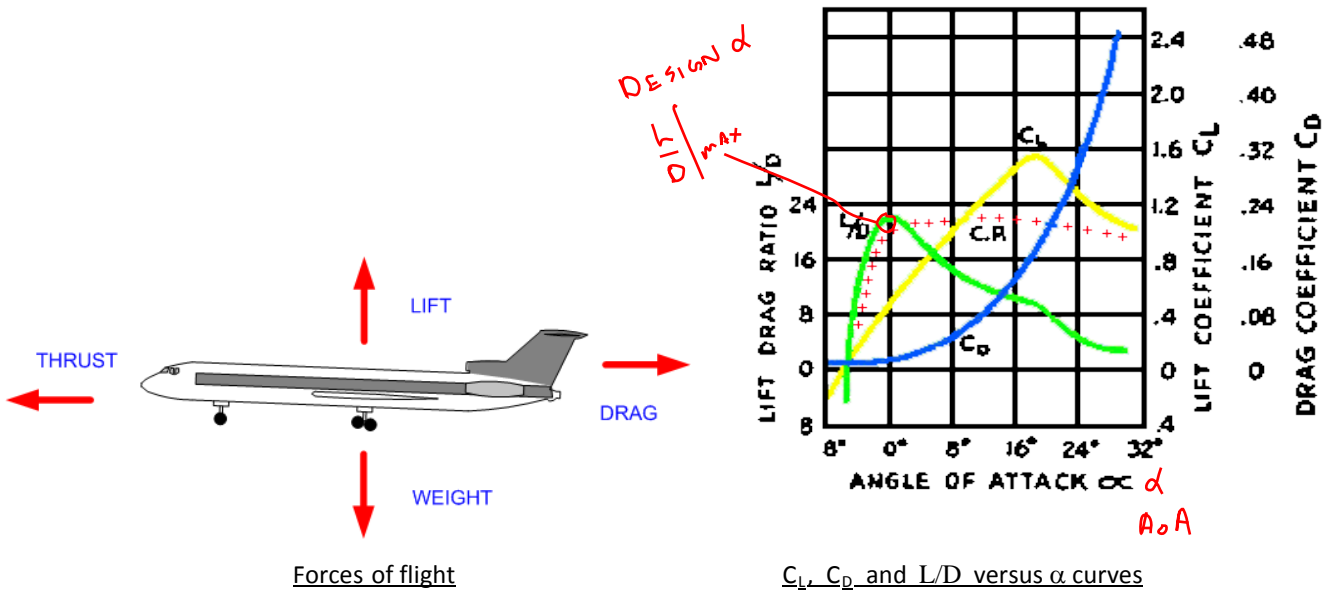
DISADVANTAGES ?



## BA 609



# Graphical representation of lift, drag, thrust and weight



$C_L$ ,  $C_D$  and  $L/D$  versus  $\alpha$  curves

$$C_L = \frac{L}{\frac{1}{2} \rho_{\infty} U_{\infty}^2 S} = \text{Lift coefficient}$$

$$C_D = \frac{D}{\frac{1}{2} \rho_{\infty} U_{\infty}^2 S} = \text{Drag coefficient}$$

$$\frac{L}{D} = \frac{C_L}{C_D} = \text{Lift-to-drag ratio}$$

where  $L$  = lift

$D$  = drag

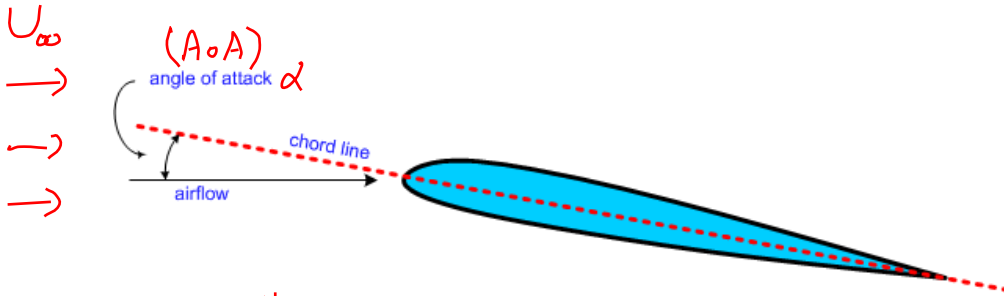
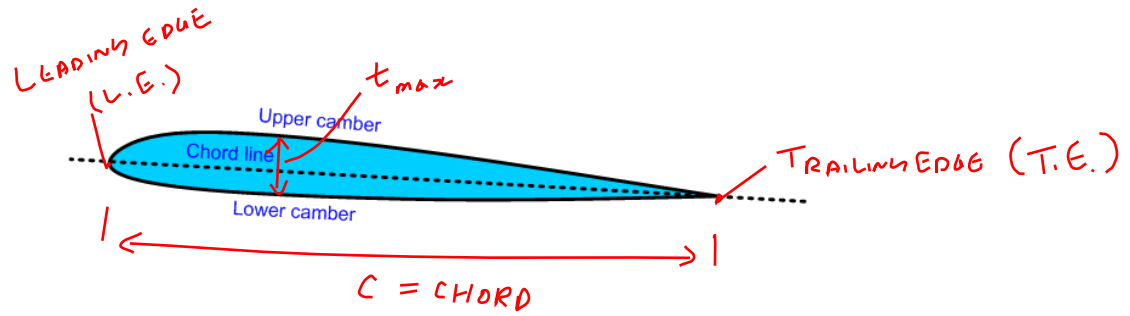
$\rho_{\infty}$  = freestream density

$U_{\infty}$  = freestream velocity

$S$  = wing area

$\frac{1}{2} \rho_{\infty} U_{\infty}^2 = P_{\text{dynamic pressure}}$

# Airfoil and Angle of attack

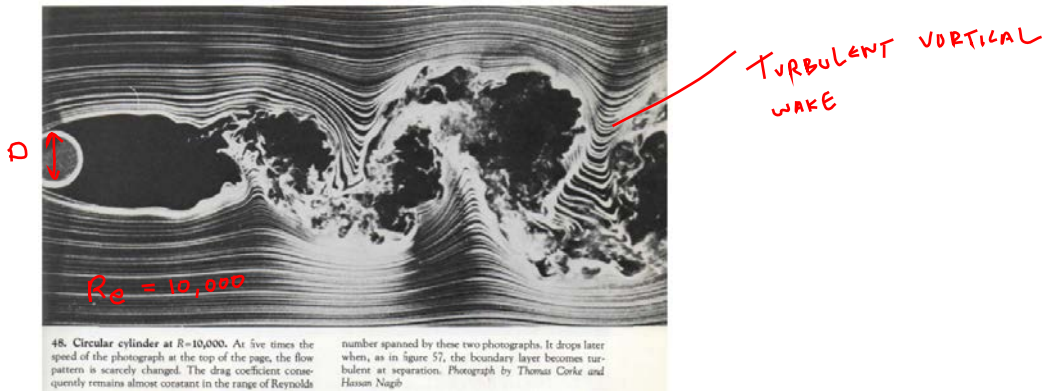


ADVISORY  
AEROSPACE  
NACA 0012 AIRFOIL: Symm. WITH  $t_{max} = 12\%c$   
NATIONAL COMMITTEE

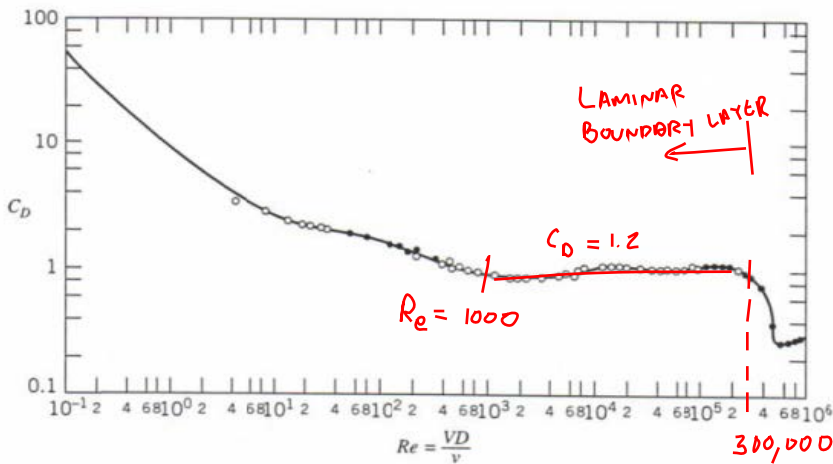
NACA 2412  
 max CAMBER POSITION @  $40\%c$   
 max CAMBER =  $2\%c$

NACA 24012  
 max CAMBER POSITION @  $\frac{40}{2}\%c$   
 DESIGN  $C_l = 2 \times \frac{3}{20} = 0.3$

# Viscous flow around a stationary circular cylinder

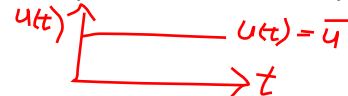


$$C_D = \frac{F_D}{\frac{1}{2} \rho_\infty U_\infty^2 A_p} = \text{drag coefficient}; \quad A_p = \text{projected area} = DL, \quad L = \text{cylinder length}$$



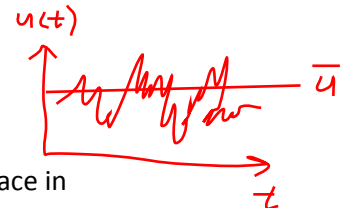
## Laminar flow:

Flow structure is characterized by motion in smooth layers. No  $\dot{m}$  or  $\dot{m}\vec{V}$  exchange between layers.



## Turbulent flow:

Flow structure is characterized by random, 3-D velocity fluctuations superimposed on the mean motion. For example,  $u(t) = \bar{u} + u'(t)$ .



## Boundary layer:

A thin layer of fluid in direct contact with or adjacent to the solid surface in which the viscosity effects of the shear stress  $\tau_{xy} = \mu \frac{du}{dy}$  is nonzero.

## Reynolds number (for viscous or real flow only)

- $Re = \frac{\text{Fluid - inertial - force}}{\text{viscous - force}} = \frac{\rho_{\infty} U_{\infty} D}{\mu}$  or  $\frac{\rho_{\infty} U_{\infty} C}{\mu}$  or  $\frac{\rho_{\infty} U_{\infty} x}{\mu}$

*DIA.* *AIRFOIL CHORD* *STREAMWISE DISTANCE / LENGTH*  
 $D, C$  and  $x \equiv$  characteristic length (of the object)

$\rho_{\infty} \equiv$  fluid density

$U_{\infty} \equiv$  fluid velocity or freestream velocity

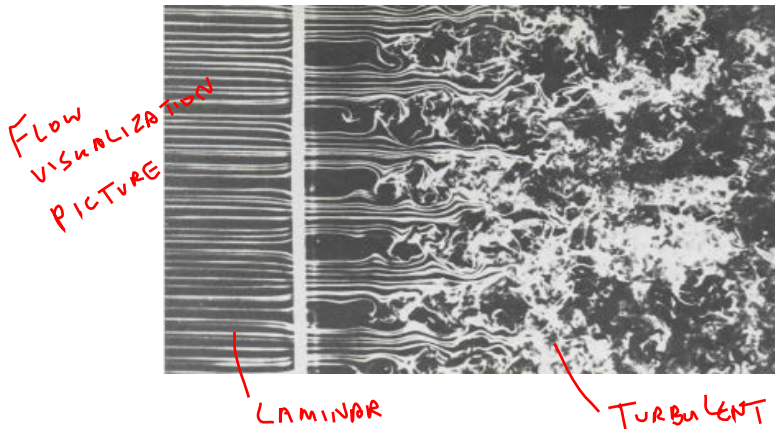
$\mu \equiv$  absolute viscosity of fluid

- Re is an indication of the state of the flow or boundary layer. *LAMINAR OR TURBULENT*
- As Re approach  $\infty$  (or very large), the flow can be treated as inviscid (i.e.,  $\mu = 0$  or ideal flow).
- For incompressible flow (i.e.  $M = \frac{U}{c} =$  Mach number  $\leq 0.3$ , where  $c$  is the speed of sound),

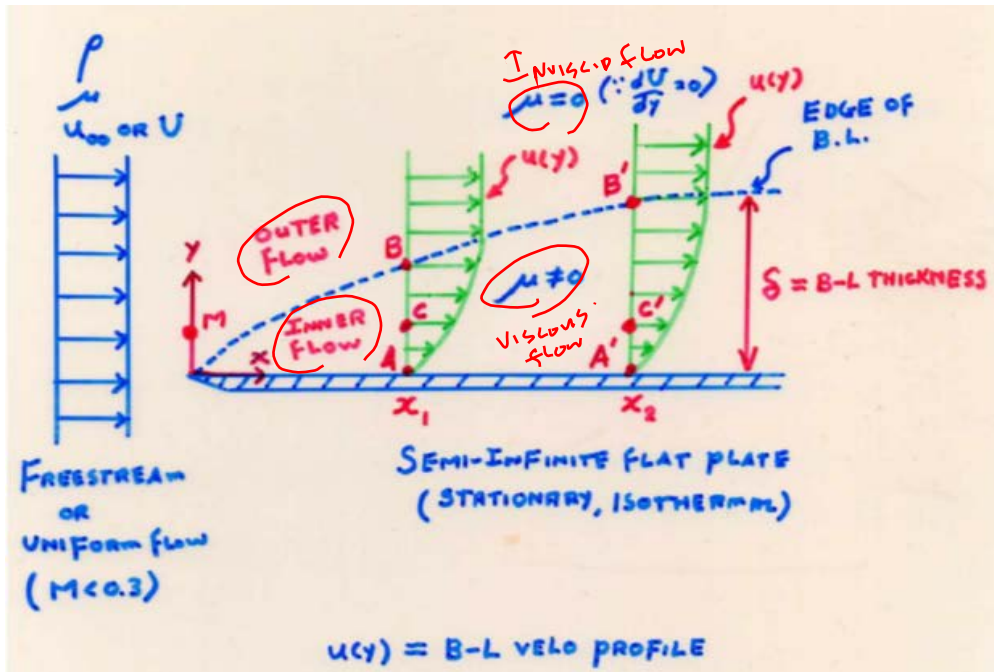
$$\nu = \frac{\mu}{\rho} = \text{kinematic viscosity}$$

*MECH 331*  $\rightarrow$  *INCOMPRESSIBLE*  
*ISOTHERMAL* *FLOW*

# Laminar and turbulent flows over a stationary flat plate



Conceptual sketch of flat-plate boundary-layer flow



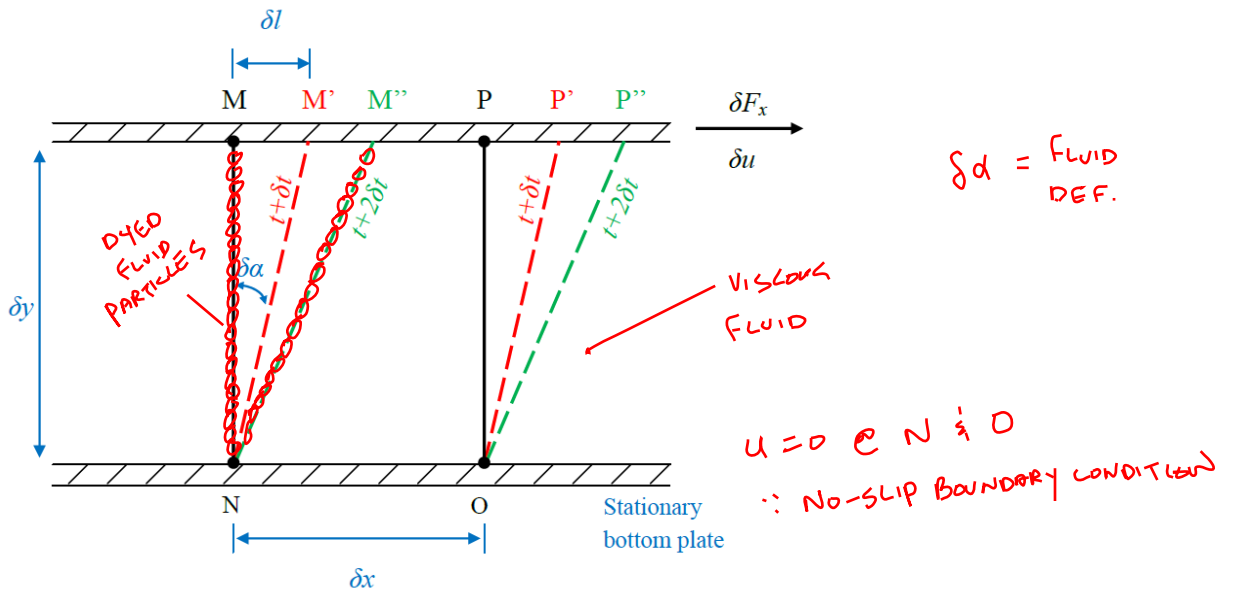
Q/A: WHY FLOW IS INVISCID FOR  $y > \delta$  ?

Q/A: IS THE E.O.B.L. A STREAMLINE ?

The Newton's law of viscosity (relate  $\frac{d\alpha}{dt}$  to  $\frac{du}{dy}$ )

RATE OF DEFORMATION

VELO GRADIENT



$$\therefore \tau_{yx} = \lim_{\delta A_y \rightarrow 0} \frac{\delta F_x}{\delta A_y} = \frac{dF_x}{dA_y} \quad \text{and} \quad \text{Deformation rate} = \lim_{\delta t \rightarrow 0} \frac{\delta \alpha}{\delta t} = \frac{d\alpha}{dt} = \frac{du}{dy}$$

where  $\delta l = du dt = dy d\alpha$  (for small angles)

$$\therefore \tau_{yx} = \mu \frac{du}{dy} \quad \text{where} \quad \mu \equiv \text{coefficient of viscous resistance} = \text{absolute viscosity}$$

Also,  $\nu = \frac{\mu}{\rho} = \text{kinematic viscosity (for incompressible flow)}$

**Timeline:** A line connects adjacent “marked or dyed” fluid particles at a given time instant in a flow field.

## Important notes

[1]  $\mu_{\text{air @ 20C}} = 1.81 \times 10^{-5} \text{ N-s/m}^2$  and  $\mu_{\text{water @ 20C}} = 1.01 \times 10^{-3} \text{ N-s/m}^2$

[2] Newtonian fluids:  $\tau_{yx} = \mu \frac{du}{dy}$  *e.g., AIR, WATER, Kerosene*

[3] Non-Newtonian fluids:  $\tau_{yx} = \kappa \left(\frac{du}{dy}\right)^n$  where  $\kappa \equiv$  consistency index *e.g., BLOOD FLOW, TOOTH PASTE*  
 $n \equiv$  flow behavior index

[4] Viscous flow (for  $\mu \neq 0$ ) and inviscid flow (for  $\mu = 0$ )

[5] All fluids possess viscosity. *REAL FLOW*  
*IDEAL / PERFECT FLOW*

[6] Definition of a fluid: A substance that deforms continuously under the application of a shear (tangential) stress  $\tau_{yx}$  no matter how small the shear stress may be.

[7] Continuum fluid mechanics (CFM)

- No gap/space between fluid particles
- Fluid properties vary smoothly from point to point
- Concept of fluid particle/element/cube

[8] Slip and no-slip boundary conditions: The relative velocity between a moving fluid and a solid boundary is non-zero for inviscid flow or zero for viscous flow. *AN EXPERIMENTAL OBSERVATION*

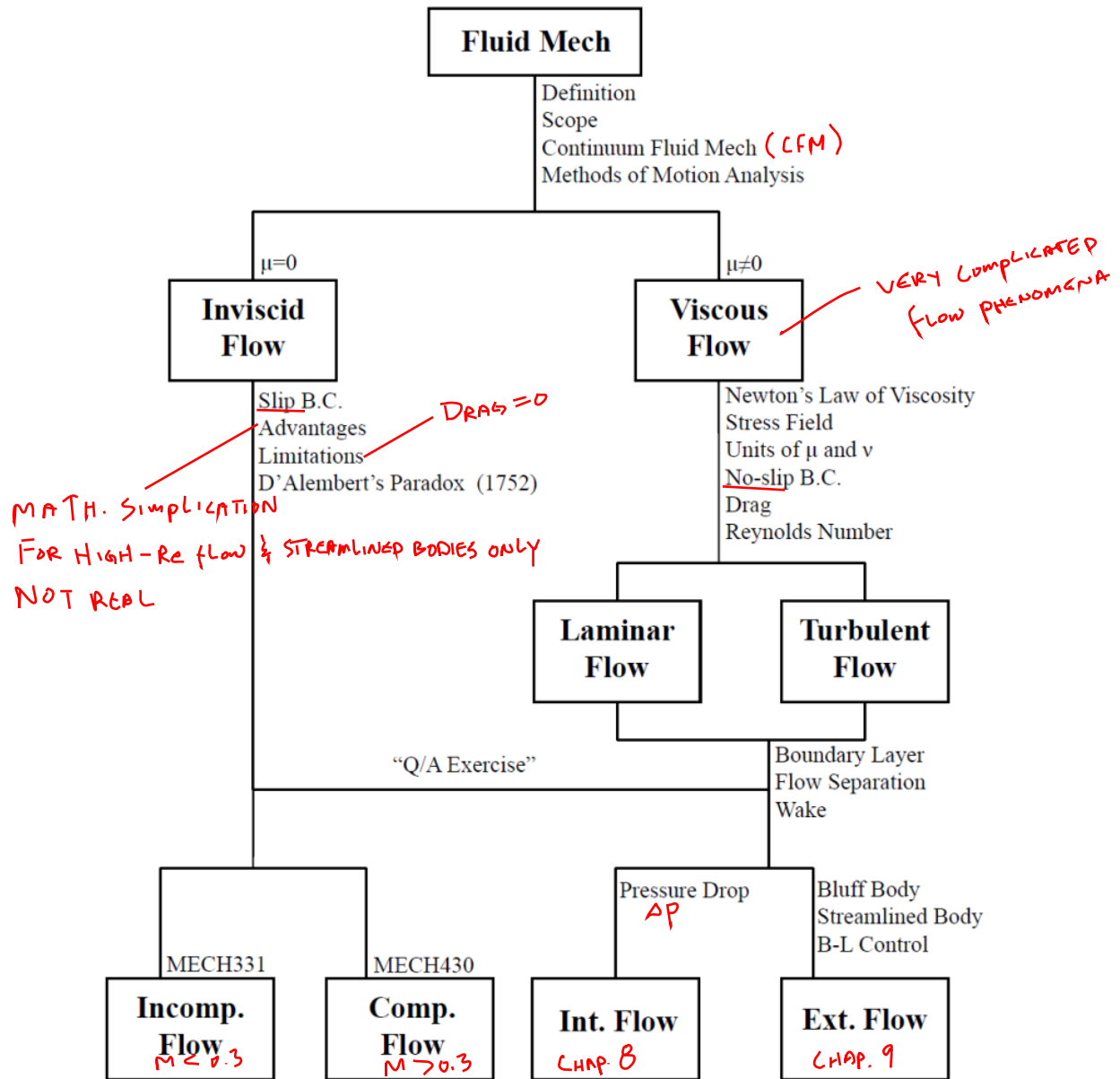
[9] D'Alembert's paradox: The aerodynamic drag on any non-lifting body of any shape is predicted to be zero when the inviscid, or irrotational, flow approximation is invoked.

*i.e.,* In real flow there is a nonzero drag on bodies immersed in a uniform stream.

[10] The significance of  $\mu$  ?

*D<sub>f</sub> ≠ 0, D<sub>p</sub> ≠ 0*  
*VISCOUS FLOW*  $\frac{1}{2}$  *INVISCID FLOW* *A SIMPLIFICATION!*  
*FORMATION OF BOUNDARY LAYER*

# Classification of fluid mechanics



## SR-71 Blackbird



$T_{SKIN}$  UP TO 1200°F ? WHY

SKIN EXPANSION  $\leq 12''$

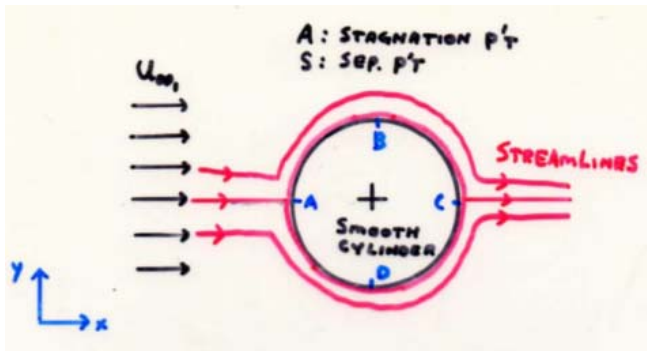
$U_c > M3.0$  @ 90,000'  
AND ABOVE

**Q/A: Why is the speed of a biplane limited to about 120 mph?**

1 mile = 5280 ft = 1.6 km

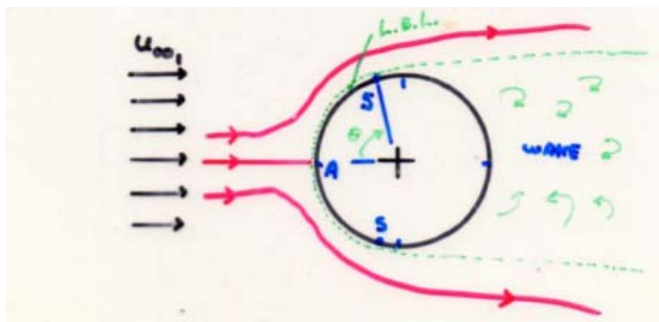


## Conceptual flow pattern over a smooth, stationary circular cylinder



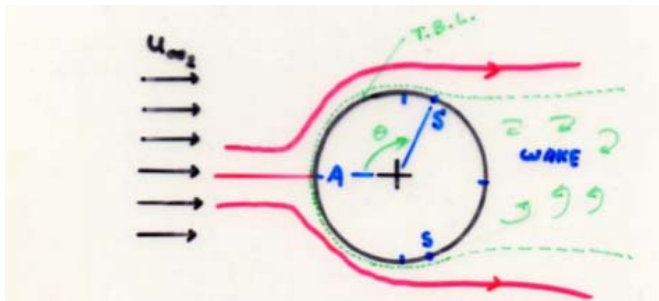
$\mu = 0$   
 $F_D = 0$   
 $F_L = 0$   
 $A \rightarrow B: \frac{dp}{dx} < 0$   
 $B \rightarrow C: \frac{dp}{dx} > 0$

Inviscid flow ( $\mu = 0$ )



$\mu \neq 0$   
 $\theta = 80^\circ$   
 $Re < 300,000$   
 $F_D \neq 0$   
 $F_L = 0$   
 LAMINAR B.L.

Viscous flow; laminar boundary layer

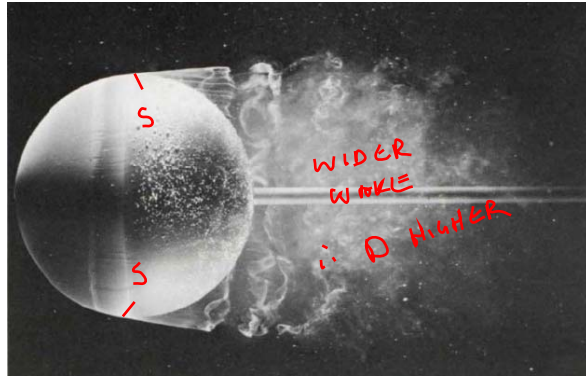


$\mu \neq 0$   
 $\theta = 120^\circ$   
 $Re > 500,000$   
 $F_D \neq 0$   
 $F_L = 0$   
 TURBULENT B.L.

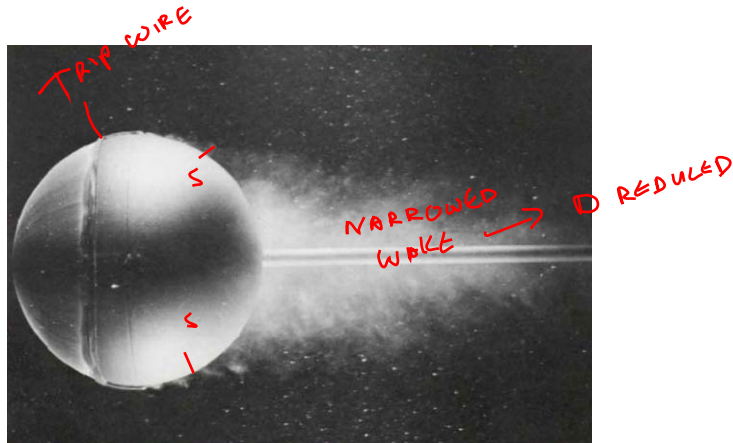
Viscous flow; turbulent boundary layer



## Smoke-flow pattern of a stationary sphere at $Re_D = 15,000$



Smooth sphere (laminar boundary layer)



With a trip wire located at around  $\theta = 70^\circ$   
(turbulent boundary layer)

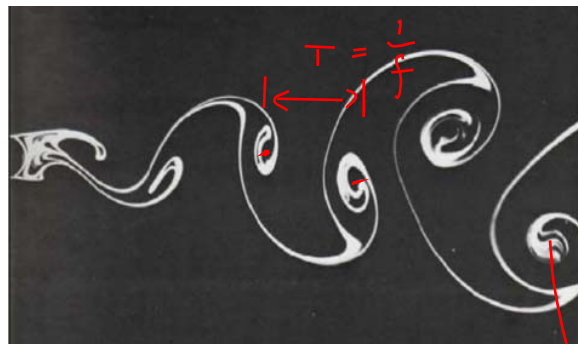
**The sudden collapse of the Tacoma Narrows bridge** (opened on July 1, 1940 and collapsed into Puget Sound on Nov. 7, 1940 under high wind conditions)



TOTAL LENGTH 9,400'  
SPAN 2,800'  
WIDTH 39', HEIGHT 470'



✓ AERDYNAMIC FLUTTER  
TURBULENCE (WIND)  
VORTEX-SHEEDING WAKE



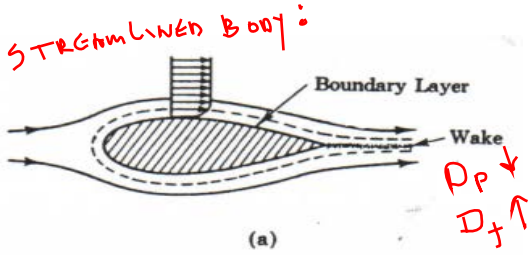
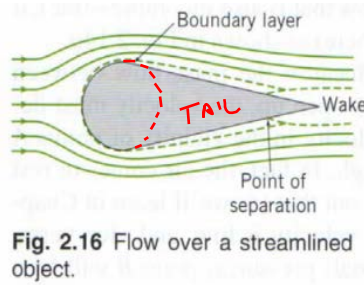
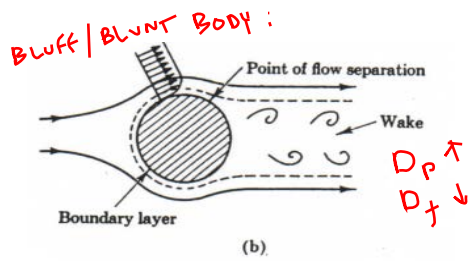
von Karman vortex shedding wake  
"NO VORTICITY, NO SOUND."

T = VORTEX SHEEDING PERIOD  
f = VORTEX-SHEEDING FREQ.

VORTICES

Q/A : WHAT IS AEGLIAN TONE ?

# Streamlining of a bluff or blunt body



Motion of fluid relative to (b) a non-streamlined object, and (a) a streamlined object

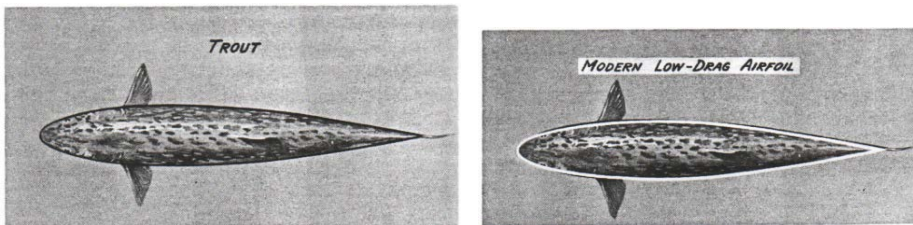
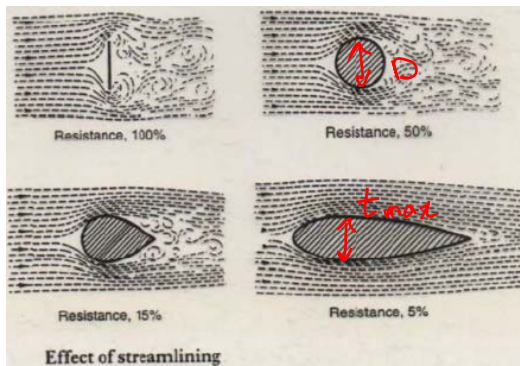


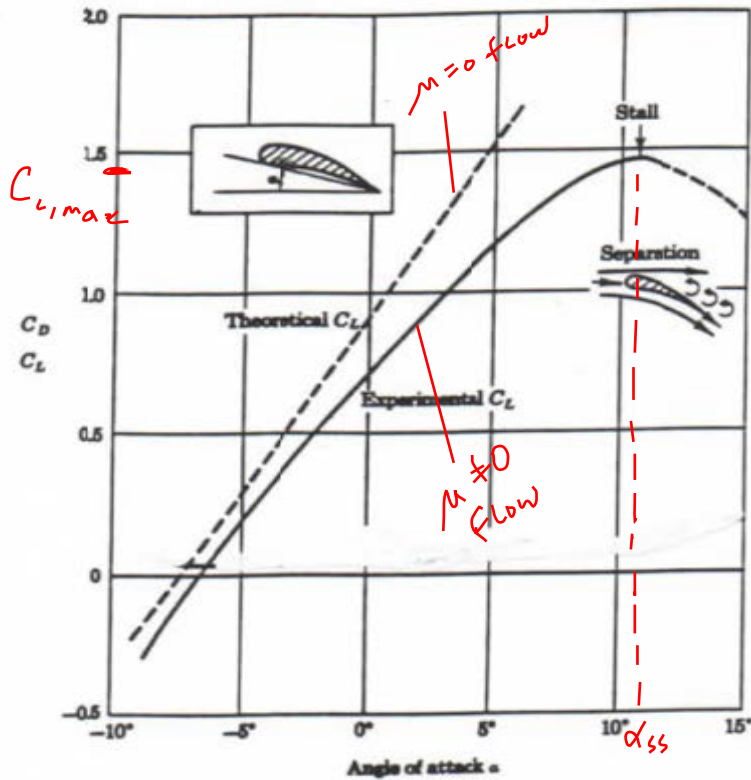
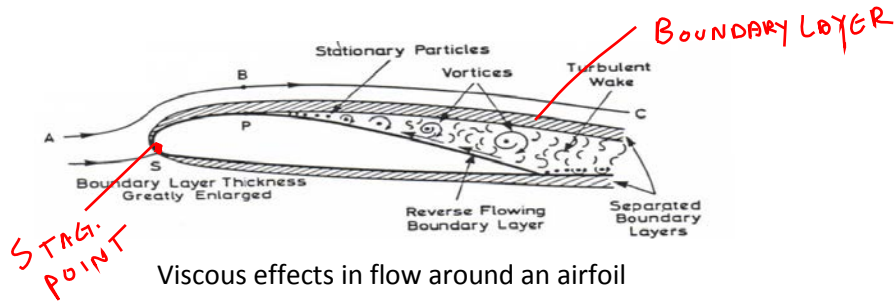
Fig. 85. Shapes of low drag can be developed not only by rational man and his intellect but also by irrational nature, through the mechanisms of gene mutation and natural selection.



$$D = t_{max}$$

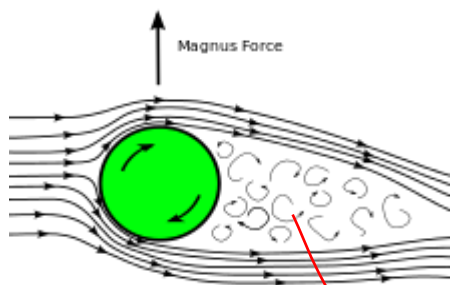
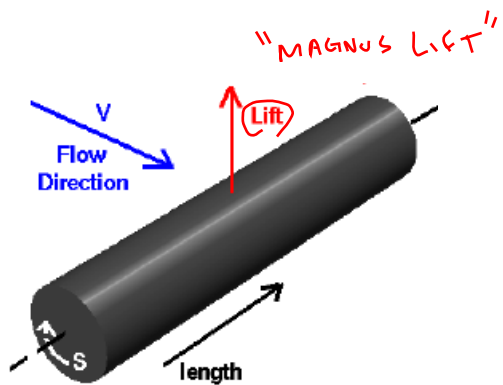
$$C_D = 1.2 \quad C_D \approx 0.06$$

## $C_L$ and $C_D$ versus $\alpha$ (angle of attack or AoA) of an airfoil



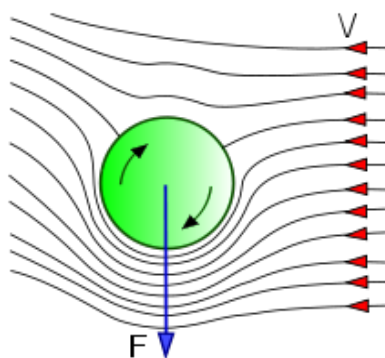
$C_L$  and  $C_D$  versus  $\alpha$  of an airfoil

# Spinning circular cylinder and Magnus Lift



$\mu \neq 0$  (Viscous flow)

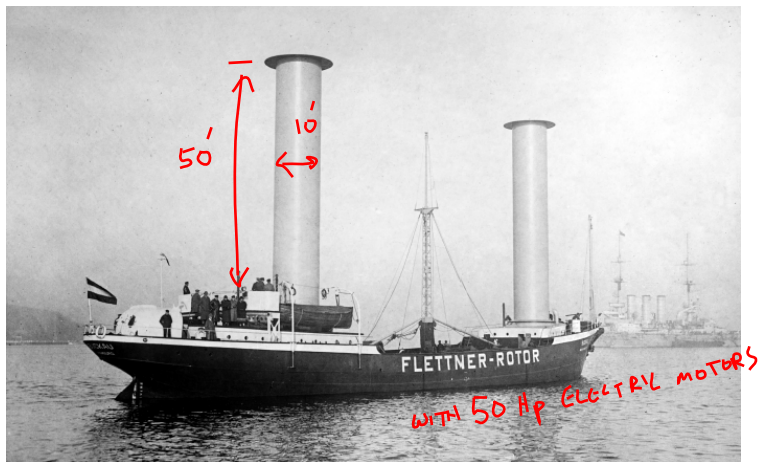
DEFLECTED WAKE (NOT SYMM.)



$\mu = 0$  (Inviscid flow)

$$\therefore \frac{P}{\rho} + \frac{V^2}{2} = \text{CONSTANT}$$

## Flettner rotor ship (1920s)



The official maiden voyage of the BUCKAU, 7 November 1924 in Kiel.

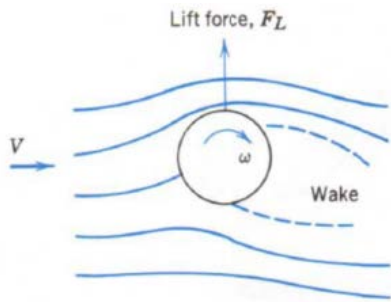


Flettner yacht on Lake Wannsee, Berlin. Photo: Anton Flettner, 1926.



E-Ship 1, August 2008

# Lift and drag coefficients of a rotating circular

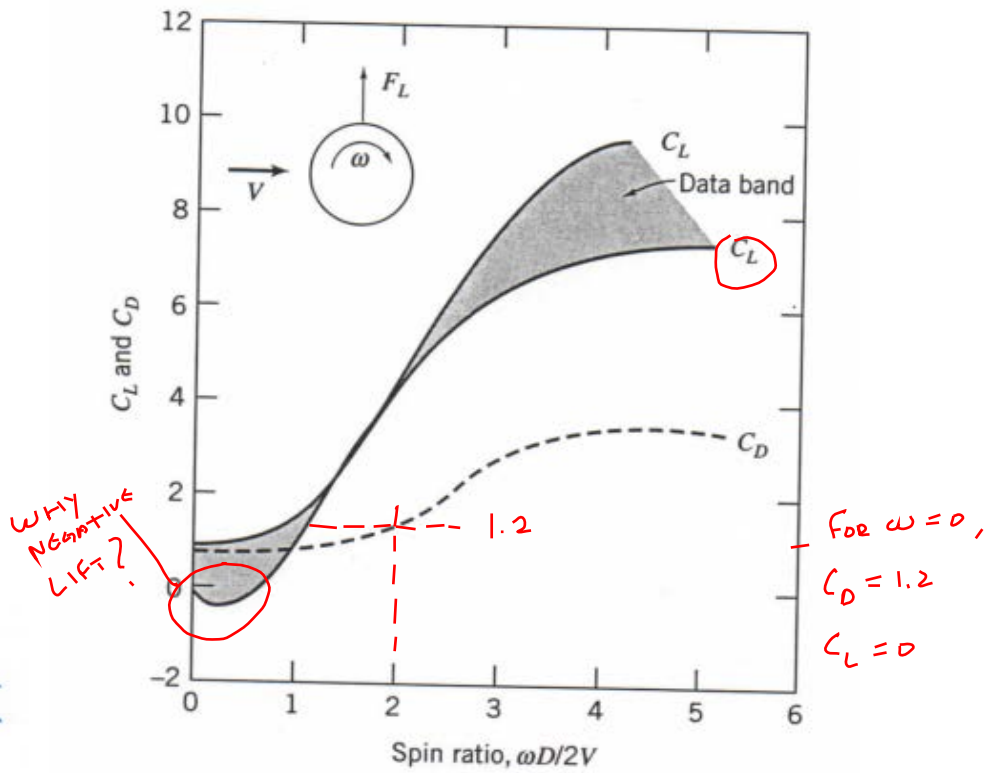


Conceptual flow pattern

where

$$C_L = \frac{F_L}{\frac{1}{2} \rho U_\infty^2 A_p}$$

$$C_D = \frac{F_D}{\frac{1}{2} \rho U_\infty^2 A_p}$$



**Fig. 9.29** Lift and drag of a rotating cylinder as a function of relative rotational speed; Magnus force. (Data from [32].)

# Flettner flying car or aircraft



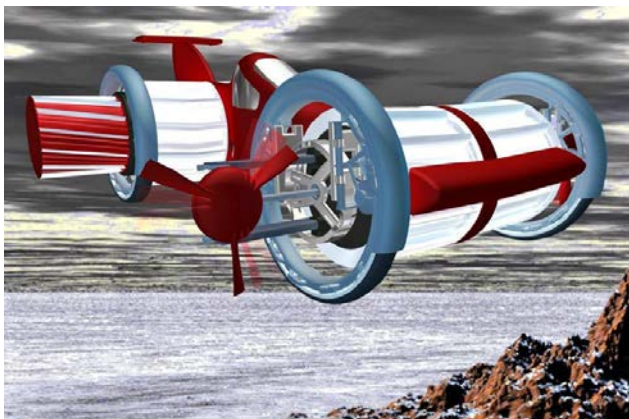
Anton Flettner's rotor aircraft

DUCTED  
FLANS  
↓  
THRUST

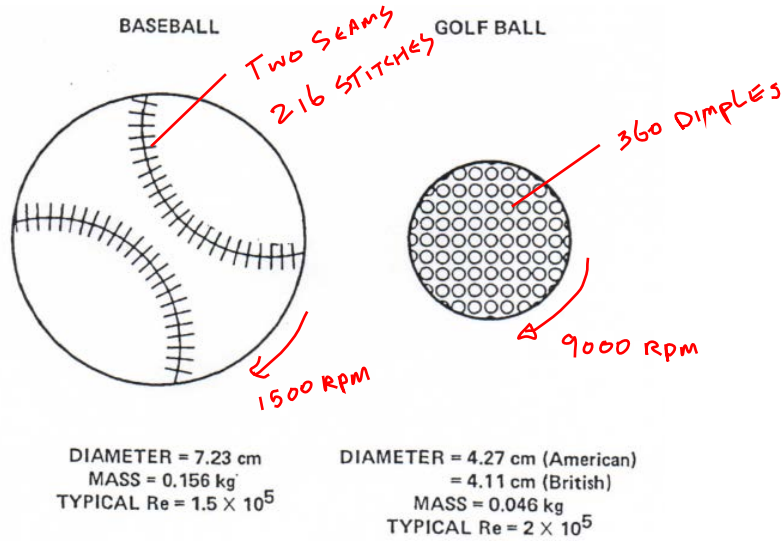


iCar 101 Ultimate 260 km/h  
1000 km RANGE

ROTATING CYLINDERS ----> LIFT  
ADVANTAGES/DISADVANTAGES?

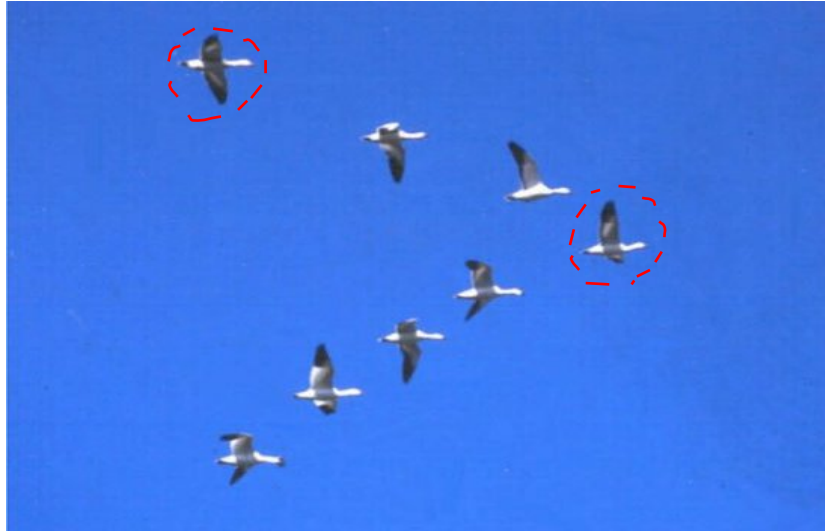


## Aerodynamics of ball sports



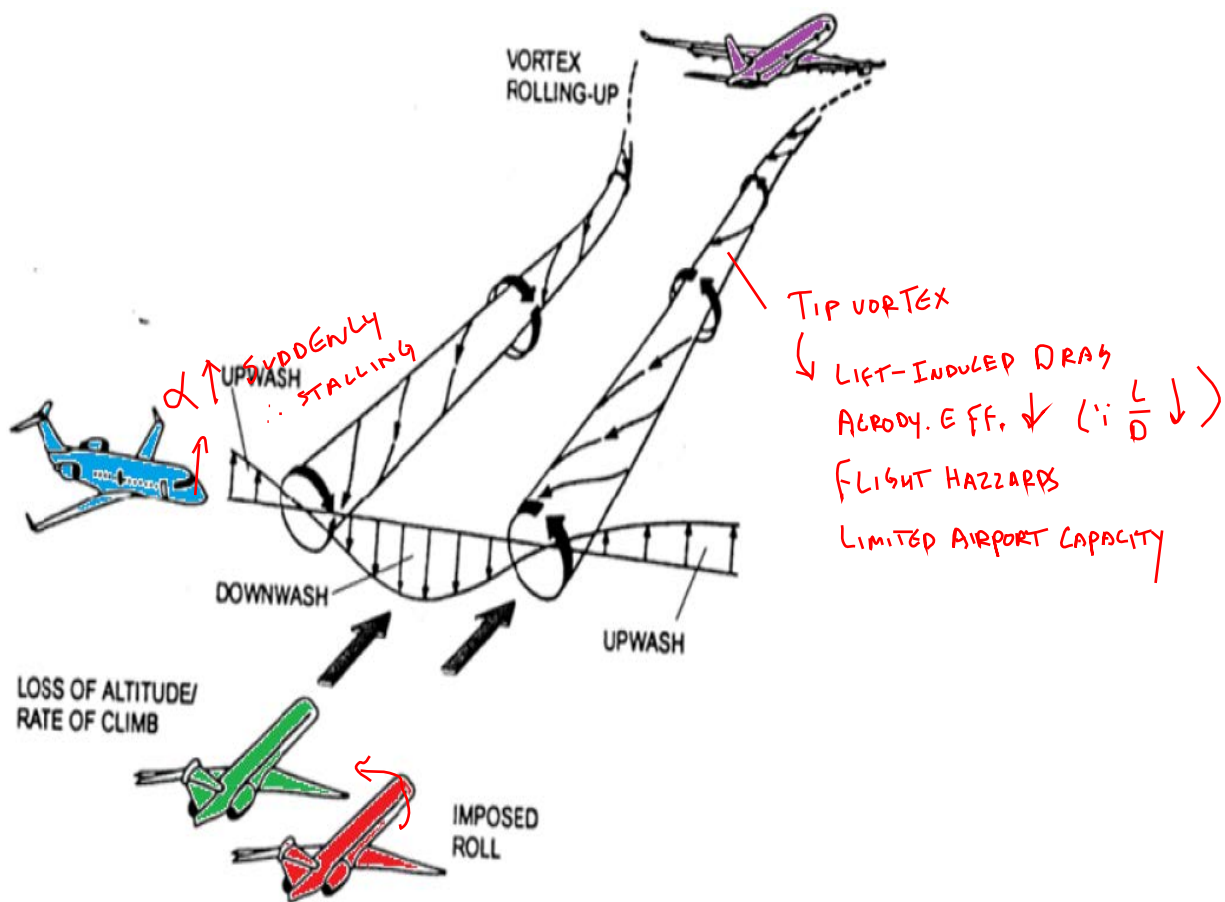
- The effects of dimples and backspin of and of a golf ball
- A curve ball
- A knuckle ball

## Geese flying in V formation



LESS ENERGY  
ADDITIONAL LIFT  
REDUCED DRAG  
FARTHER DISTANCE  
WHY ? ?

## Wingtip vortices and flight hazards



# Winglets

Learjet 45



A320NEO 2130 FIRM ORDERS



B737MAX ~1325 FIRM ORDERS

