

4.38

A piston cylinder contains 1 kg of liquid water at 20°C and 300 kPa, as shown in Fig. P4.38. There is a linear spring mounted on the piston such that when the water is heated the pressure reaches 3 MPa with a volume of 0.1 m³.

- Find the final temperature
- Plot the process in a P-v diagram.
- Find the work in the process.

Solution:

Take CV as the water. This is a constant mass:

$$m_2 = m_1 = m ;$$

State 1: Compressed liquid, take saturated liquid at same temperature.

$$\text{B.1.1: } v_1 = v_f(20) = 0.001002 \text{ m}^3/\text{kg},$$

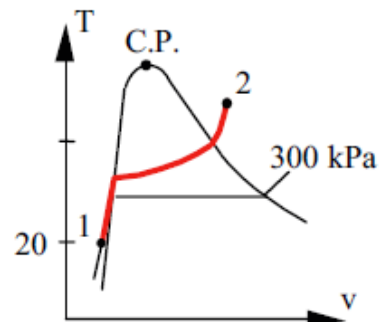
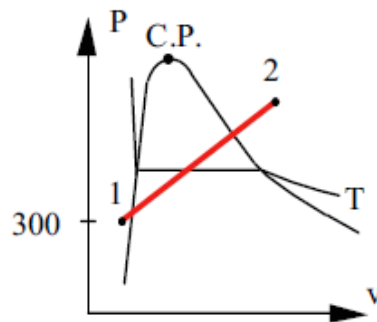
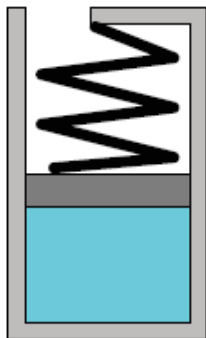
State 2: $v_2 = V_2/m = 0.1/1 = 0.1 \text{ m}^3/\text{kg}$ and $P = 3000 \text{ kPa}$ from B.1.3

=> Superheated vapor close to $T = 400^\circ\text{C}$

$$\text{Interpolate: } T_2 = 404^\circ\text{C}$$

Work is done while piston moves at linearly varying pressure, so we get:

$$\begin{aligned} {}_1W_2 &= \int P \, dV = \text{area} = P_{\text{avg}} (V_2 - V_1) = \frac{1}{2} (P_1 + P_2)(V_2 - V_1) \\ &= 0.5 (300 + 3000)(0.1 - 0.001) = 163.35 \text{ kJ} \end{aligned}$$



4.72

10 kg of water in a piston cylinder arrangement exists as saturated liquid/vapor at 100 kPa, with a quality of 50%. It is now heated so the volume triples. The mass of the piston is such that a cylinder pressure of 200 kPa will float it, see Fig. P4.72.

- Find the final temperature and volume of the water.
- Find the work given out by the water.

Solution:

Take CV as the water $m_2 = m_1 = m$;

Process: $v = \text{constant}$ until $P = P_{\text{liff}}$ then P is constant.

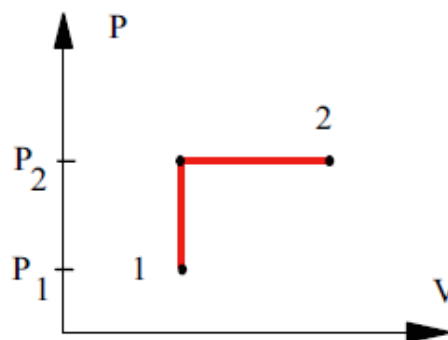
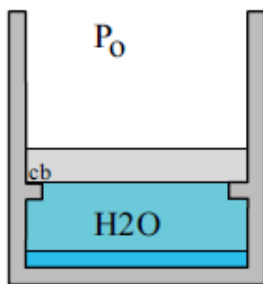
State 1: $v_1 = v_f + x v_{fg} = 0.001043 + 0.5 \times 1.69296 = 0.8475 \text{ m}^3/\text{kg}$

State 2: $v_2, P_2 \leq P_{\text{liff}} \Rightarrow v_2 = 3 \times 0.8475 = 2.5425 \text{ m}^3/\text{kg}$;

$T_2 = 829^\circ\text{C}$; $V_2 = m v_2 = 25.425 \text{ m}^3$

$${}_1W_2 = \int P dV = P_{\text{liff}} \times (V_2 - V_1)$$

$$= 200 \text{ kPa} \times 10 \text{ kg} \times (2.5425 - 0.8475) \text{ m}^3/\text{kg} = 3390 \text{ kJ}$$



4.124

A cylinder fitted with a piston contains propane gas at 100 kPa, 300 K with a volume of 0.2 m^3 . The gas is now slowly compressed according to the relation $PV^{1.1} = \text{constant}$ to a final temperature of 340 K. Justify the use of the ideal gas model. Find the final pressure and the work done during the process.

Solution:

The process equation and T determines state 2. Use ideal gas law to say

$$P_2 = P_1 \left(\frac{T_2}{T_1} \right)^{\frac{n}{n-1}} = 100 \left(\frac{340}{300} \right)^{\frac{1.1}{0.1}} = 396 \text{ kPa}$$

$$V_2 = V_1 \left(\frac{P_1}{P_2} \right)^{1/n} = 0.2 \left(\frac{100}{396} \right)^{1/1.1} = 0.0572 \text{ m}^3$$

For propane Table A.2: $T_c = 370 \text{ K}$, $P_c = 4260 \text{ kPa}$, Figure D.1 gives Z.

$$T_{r1} = 0.81, P_{r1} = 0.023 \Rightarrow Z_1 = 0.98$$

$$T_{r2} = 0.92, P_{r2} = 0.093 \Rightarrow Z_2 = 0.95$$

Ideal gas model **OK** for both states, minor corrections could be used. The work is integrated to give Eq.4.4

$$\begin{aligned} {}_1W_2 &= \int P \, dV = \frac{P_2V_2 - P_1V_1}{1-n} = \frac{(396 \times 0.0572) - (100 \times 0.2)}{1 - 1.1} \text{ kPa m}^3 \\ &= -26.7 \text{ kJ} \end{aligned}$$