

### Econ 301: Assignment 1

Instructor: Szilvia Pápai, Concordia University  
due 1:15p.m., January 23, 2013, in class

*Please show all the necessary calculations and explanations that lead to your answer. Provide your answers in the order the problems are given.*

1. (6 points) TRUE or FALSE. Determine if each of the following statements is true or false. Explain your reasoning. All credits are given for explanations.
  - a. In a two-good model, the consumer is worse off if income is reduced by half and if both prices decrease by half.
  - b. Indifference curves representing different levels of preference can cross each other.
  - c. Convex preferences mean that averages are preferred to extremes.
2. (10 points) Suppose the consumer consumes two goods: hamburgers and CDs. Her monthly income is  $m = \$400$ . The price of a hamburger is  $p_1 = \$5$  and the price of a CD is  $p_2 = \$20$ .
  - a. Write down her monthly budget constraint. Illustrate graphically the budget set. Calculate the slope of the budget line.
  - b. Suppose the government levies a 25% tax on each CD the consumer purchases. What is the new monthly budget constraint? Draw the new budget line.
  - c. Now suppose that instead of the 25% tax on CDs each consumer pays a fixed sum of \$100 in taxes per month. What is the monthly budget constraint in this case? Draw the new budget line.
  - d. Now suppose that there is no tax of any kind; instead, assume that our consumer lives in a country where the government acts as a health police and rations hamburgers. In this country, each consumer is allowed to eat at most 60 hamburgers per month. What is the monthly budget constraint in this case? Draw the new budget line.
3. (10 points) Art is a history major. He has to take two courses, one in philosophy and the other in mathematics. He is relatively good at philosophy, but not so much at math. He needs to spend 1 hour studying for philosophy in order to improve his grade by one point, while he needs to spend 2 hours studying for math in order to do the same. Art has a total of 40 hours to study for the two subjects. Suppose that he would get 50 points in each course if he didn't study at all.
  - a. We want to analyze Art's problem with consumption theory. What are the goods, prices, and income? Write down the budget constraint.

Illustrate it with a graph. (Hint: consider the *improvements* on Art's grades. That is, the goods are improvements in philosophy and math, and the prices are the cost of improvement measured in hours.)

- b. Now suppose that Art has to pass both subjects by obtaining at least 60 points in both courses. Illustrate his new budget set in a graph.

4. (8 points)

- a. Consider a group of people and the relation "at least as old as." Is this relation transitive? Is it complete?
- b. Consider a group of people and the relation "older than." Is this relation transitive? Is it complete?  
Explain all your answers.

5. (16 points) Jon likes both mangoes and bananas. For him 2 bananas are "worth" one mango, so that he is indifferent among the bundles  $(6, 0)$ ,  $(4, 1)$ ,  $(2, 2)$  and  $(0, 3)$ , for example, where each bundle is given as  $(x_b, x_m)$ , and  $x_b$  denotes the amount of bananas, while  $x_m$  denotes the amount of mangoes.

- a. Find some bundles such that Jon is indifferent between these and the bundle  $(8, 0)$ .
- b. Plot some of Jon's indifference curves in a graph.
- c. What is the MRS for these indifference curves at different points? Do these indifference curves exhibit a diminishing marginal rate of substitution?
- d. Are Jon's preferences monotonic?