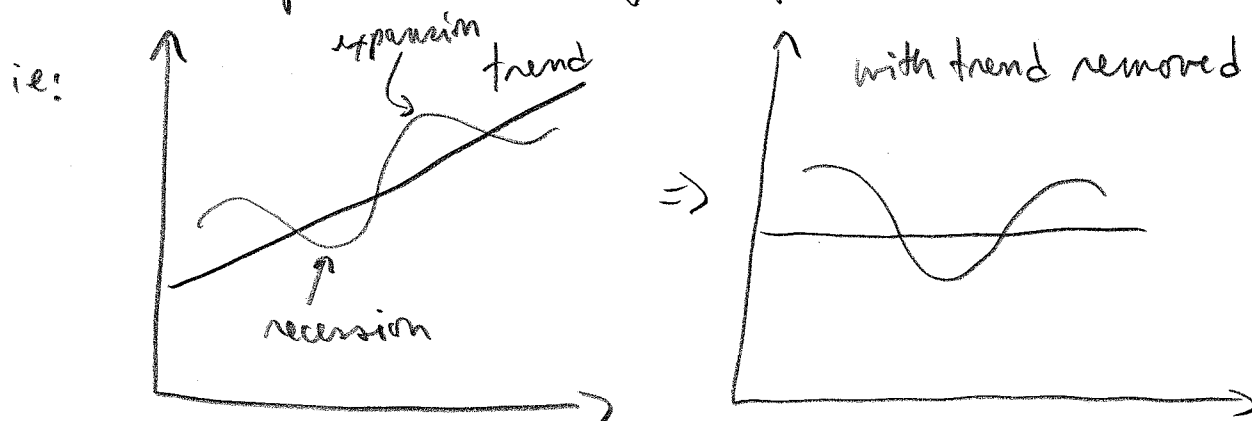


→ The model we look at so far aims at explaining the source of business cycle fluctuations



→ ultimately, whether a model can be used to explain what is actually happening in the "real world" is an empirical matter

↳ we have to compare the model's predictions to what we observe in the data

→ economists usually evaluate models in several dimensions of the data. We will limit our investigation to correlations

↳ measure of statistical association between two variables

→ we will look at correlations over time

↳ macro focuses on the time dimension. Our one period model is not suited to look at macro issues but we can still try to learn something from it.

# Correlations

→ measured by the correlation coefficient

$$\rho = \frac{\text{cov}(x, y)}{\sqrt{\text{Var}(x) \cdot \text{Var}(y)}}$$

→ covariance between x and y

↑ variability of x

↑ variability of y

↳  $\rho$  is between -1 and 1.

perfect negative correlation

x and y always move in opposite direction

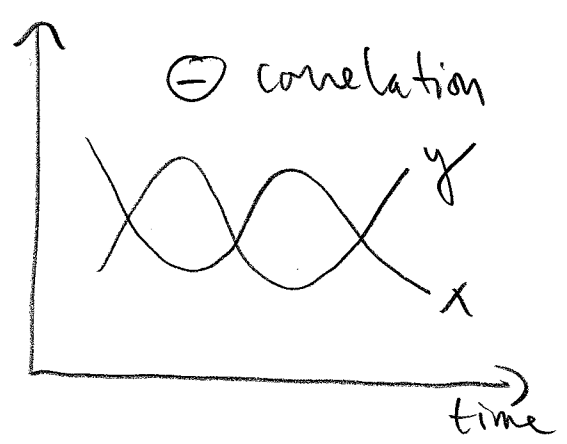
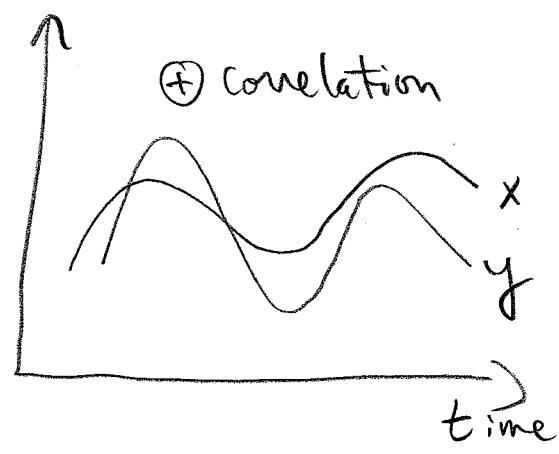
perfect positive correlation

x and y always move in the same direction

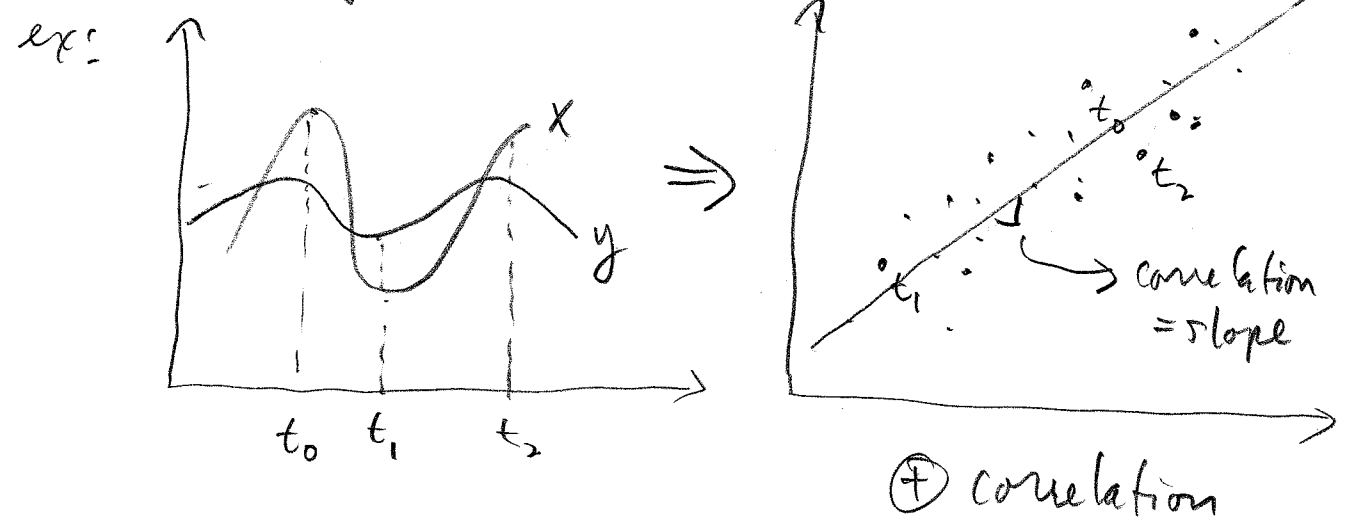
→ when  $\rho = 0$ , x and y are uncorrelated

↳ do not move together  
(no systematic relationship between x and y)

ex:  
association between x and y over time



another way to look at correlations is to graph one variable against the other



note: a variable which has a positive correlation with real GDP is pro cyclical

ex:

↳ moves with the business cycle

• a variable which has a negative correlation with real GDP is countercyclical

↳ moves opposite to the cycle

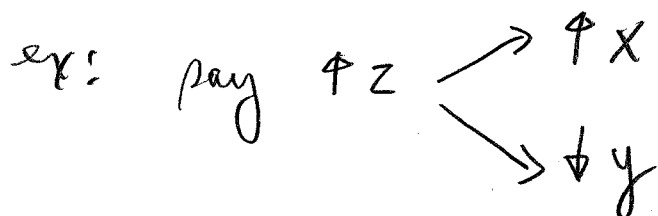
• a variable not correlated with GDP is acyclical

↳ this is along this dimension that we will look at the predictions of our one-period model compared to "reality"

a word of caution:

→ a correlation is not an indication of causality. IF  $x$  and  $y$  are correlated, it does not mean that movements in  $x$  cause those in  $y$  (or vice versa)

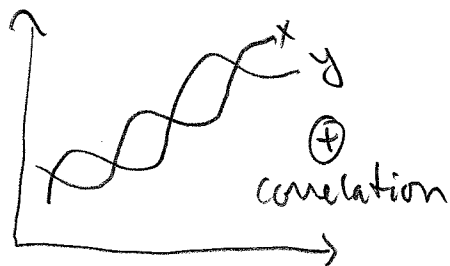
↳ correlations only measure "statistical" association. only theory can indicate causality.



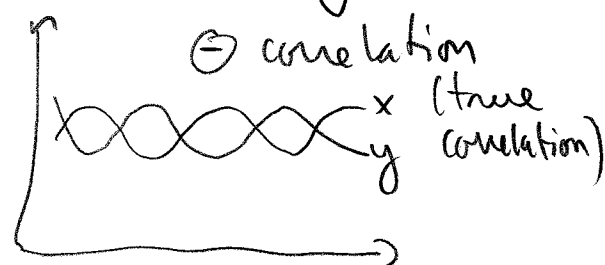
but  $x$  and  $y$  are not related

↳ if the correlation between  $x$  and  $y$  is calculated, it will be positive. However, changes in  $x$  does not cause changes in  $y$  (or vice versa). It is  $z$  that causes movements in both variables.

→ correlations work only for stationary variables



but



Let's look at the correlations predicted by our one period model:

what can be the source of business cycle fluctuations in this model?

↳ must come from variations in exogenous variables

ie:  $\Delta G$  or  $\Delta Z$

only movements in those variables can cause variations in  $C, N, Y$  and  $w$

Recall: predictions of the model

$$\uparrow G \rightarrow \begin{cases} \downarrow C & (\uparrow T \rightarrow \downarrow \text{disposable income}) \\ \uparrow N & (\downarrow l : l \text{ and } C \text{ are normal goods}) \\ \uparrow Y & (\text{because } N \uparrow) \\ \downarrow w & (\uparrow N \rightarrow \downarrow MPN : w = MPN) \end{cases}$$

$$\uparrow Z \rightarrow \begin{cases} \uparrow C & (\text{because income } \uparrow) \\ \uparrow \downarrow N? & \text{substitution or income effect?} \\ \uparrow Y & [\uparrow Z \rightarrow \uparrow Y \rightarrow \uparrow C] \\ \uparrow w & [\uparrow Z \rightarrow \uparrow MPN] \end{cases}$$

look at graphs:  $\Delta G$  cannot "cause" the business cycle because  $C$  is procyclical and  $\uparrow G \rightarrow \uparrow Y \rightarrow \downarrow C$

⑥

→  $\Delta z$  seems a better candidate (see graph)

- income effect seem to dominate change in hours but employment (the number of people employed) is procyclical

↳ seems more important to explain (un)employment than movement in hours worked

note: the theory in which  $\Delta z$  produces  $\Delta y$  is called "Real Business Cycle" theory (RBC)

↳ source of cycles are "real", (here, productivity changes) from the supply side of the economy, rather than from demand fluctuations (ie:  $\Delta G$ )

↳ how do we "measure"  $z$ ? (not observable)

$$Y = zK^{\alpha}N^{1-\alpha} \Rightarrow z = \frac{\overset{\text{observable}}{Y}}{\underbrace{K^{\alpha}N^{1-\alpha}}_{\text{observable}} = 1/3}$$

This is called "Solow Residual"